## Transformations of Functions

note: $c>0$

$f(x)+c$ shifts the graph of $f(x)$ up $c$ units $f(x)-c$ shifts the graph of $f(x)$ down $c$ units

$f(x+c)$ shifts the graph of $f(x)$ left $c$ units $f(x-c)$ shifts the graph of $f(x)$ right $c$ units

$-f(x)$ reflects the graph of $f(x)$ about the $x$-axis

$f(-x)$ reflects the graph of $f(x)$ about the $y$-axis

$c \cdot f(x)\left\{\begin{array}{l}\text { stretches } f(x) \text { vertically by } c \text { if } c>1 \\ \text { squeezes } f(x) \text { vertically by } c \text { if } 0<c<1\end{array}\right.$

$f(c \cdot x)\left\{\begin{array}{l}\text { squeezes } f(x) \text { horizontally by } c \text { if } c>1 \\ \text { stretches } f(x) \text { horizontally by } c \text { if } 0<c<1\end{array}\right.$

